# Warm-up

1. We know that every circle is similar, is every sphere similar?
2. Find the volume of a sphere with a 12 in radius. Leave your answer in terms of π.
3. Find the volume of a sphere with a 3 in radius. Leave your answer in terms of π.
4. Find the scale factor of the spheres from #2 and #3. Then find the ratio of the volumes and reduce it. What do you notice?
5. Two squares have a scale factor of 2:3. What is the ratio of their areas?
6. The smaller square from #5 has an area of 16 cm^2. What is the area of the larger square?
7. The ratio of the areas of two similar triangles is 1:25. The height of the larger triangle is 20 cm, what is the height of the smaller triangle?

10.4 Similarity and volume

Know What? Your mom and dad have cylindrical coffee mugs with the dimensions to the right. Are the mugs similar? (You may ignore the handles.) If the mugs are similar, find the volume of each, the scale factor and the ratio of the volumes.
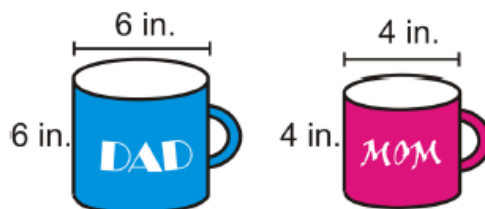
Recall that two shapes are similar if all the corresponding angles are congruent and the corresponding sides are proportional.

Similar Solids: Two solids are similar if and only if they are the same type of solid and their corresponding linear measures (radii, heights, base lengths, etc.) are proportional.

Example 1: Are the two rectangular prisms similar? How do you know?
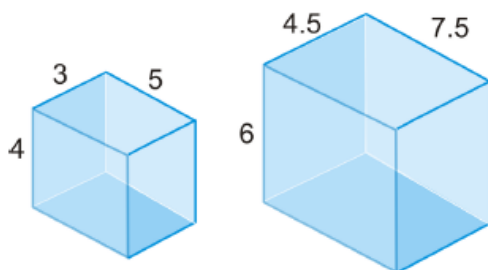
Example 2: Determine if the two triangular pyramids similar.
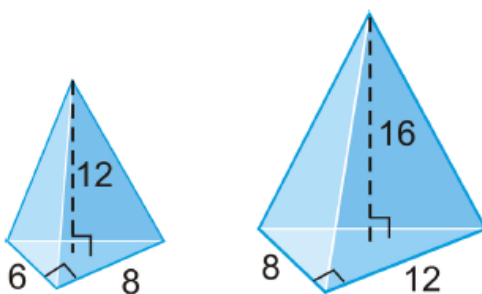
Volumes of Similar Solids

Let's look at what we know about similar solids so far.

TABLE 2.3:

	Ratios	Units
Scale Factor	$\frac{a}{b}$	in, ft, cm, m, etc.
Ratio of the Surface Areas	$\left(\frac{a}{b}\right)^2$	in^2, ft^2, cm^2, m^2, etc.
Ratio of the Volumes	??	in^3, ft^3, cm^3, m^3, etc.

Is there a pattern forming? If so what is it?

Example 7: Two spheres have radii in a ratio of 3:4. What is the ratio of their volumes?

Example 8: If the ratio of the volumes of two similar prisms is 125:8, what is their scale factor?

Example 9: Two similar right triangle prisms are below. If the ratio of the volumes is 343:125, find the missing sides in both figures.
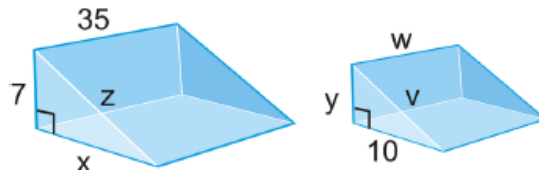
5. Are all cubes similar? Why or why not?
6. Two prisms have a scale factor of 1:4. What is the ratio of their surface areas?
7. Two pyramids have a scale factor of 2:7. What is the ratio of their volumes?
8. Two spheres have radii of 5 and 9. What is the ratio of their volumes?
9. The surface area of two similar cones is in a ratio of 64:121. What is the scale factor?
10. The volume of two hemispheres is in a ratio of 125:1728. What is the scale factor?
11. A cone has a volume of 15π and is similar to another larger cone. If the scale factor is 5:9, what is the volume of the larger cone?
12. A cube has sides of length x and is enlarged so that the sides are $4x$. How does the volume change?
13. The ratio of the volumes of two similar pyramids is 8:27. What is the ratio of their total surface areas?
14. The ratio of the volumes of two tetrahedrons is 1000:1. The smaller tetrahedron has a side of length 6 cm. What is the side length of the larger tetrahedron?
15. The ratio of the surface areas of two cubes is 64:225. If the volume of the smaller cube is 13824 m^3, what is the volume of the larger cube?